# A Method to Improve Stability of Adaptive Steering Driver-Vehicle Systems

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*Abstract*: We have developed an adaptive steering controller achieving good tracking performance. However, we have designed an ideal vehicle model in disregard of the variations of the driver properties. For the variations of the driver properties, if an adequate ideal vehicle model can be designed, the better handling stability of the adaptive driver-combined-vehicle systems can be realized. In this paper, we propose a scheme to design an ideal vehicle model adequate for the variations of the driver properties. Finally, it is shown by carrying out numerical simulations that the designed ideal vehicle model is very effective.

Keywords: Steering Control, Adaptive Control, Model Following Control

## **I. INTRODUCTION**

To improve handling stability of combined vehicles, the three states, the combination angle, the lateral velocity and yaw rate of tractor, must be controlled with three independent control inputs. Recently, the researches of steer-by-wire, are conducted actively<sup>[1]</sup>. Using the technology of steer-by-wire, the three steering angles such as the steering angle of the trailer, the front and rear steering angle of the tractor can be used as the independent control inputs possibly. Based on the notion, control schemes have been proposed <sup>[2,3]</sup> in which three independent steering control inputs are used. However, these proposed controllers require all accurate knowledge of combined vehicle parameter.

To straggle with the problem stated above, the authors have proposed robust steering control schemes<sup>[4,5]</sup>. In the schemes, an ideal vehicle model is designed, and then, the steering controller is developed so that the actual vehicle tracks the ideal vehicle model even if the large parameter variation occurs in the vehicle dynamics. In the proposed schemes, however, an ideal vehicle model is designed in disregard of the variations of the driver properties. Therefore, the authors have proposed a design scheme for ideal vehicle models<sup>[6,7]</sup> adequate for the variations of the deriver properties. In the scheme, several ideal vehicle models are designed against the variation of the driver properties and the ideal vehicle model has to be changed according to the variation. For this reason, the scheme proposed in [6,7] require accurate information of the variation of the driver properties. In addition, there exists the problem that the construction of controller becomes too complex.

In this paper, we propose a new design scheme for an ideal vehicle model. A design method based on a cost function is proposed and only one ideal vehicle model is



Fig.1 Tractor-semitrailer model

designed. In the designed ideal vehicle model, the rough information of the variation of the driver properties is only required. Carrying out numerical simulations, for the variation of the driver properties, it is shown that the adaptive steering controller using the proposed ideal vehicle model has good effectiveness.

## $\blacksquare$ . INTRODUCTION

In this paper, a simplified bicycle model of tractorsemitrailers shown in Figure 1 is used to design an adaptive steering controller. In Figure 1, the point C.G. is the center of gravity, and the point P is the reference point. Definitions for parameters of combined vehicles are shown in Table 1.

The following assumptions are made to develop a controller for the combined vehicles shown in Fig.1.

- A1 Lateral velocity of tractor  $v_p(t)$ , yaw rate of tractor  $\gamma_1(t)$ , combination yaw rate  $\dot{\varepsilon}_c(t)$  and combination angle  $\varepsilon_c(t)$  can be measured.
- A2 The length  $d_p$ ,  $l_f$ ,  $l_r$  and the length of trailer  $l_t$  are known. The other parameters include uncertainties.
- A3 Longitudinal velocity  $v_x$  is a bounded constant and available.

The dynamic equation of combined vehicle can be described as follows.

Table	1 Notation of tractor-semitrailer model
$v_x$	longitudinal velocity of tractor
$v_p, v_c$	lateral velocity of tractor at P and C.G.
$\mathcal{E}_1, \mathcal{E}_2$	yaw angles of tractor and trailer
$\mathcal{E}_{c}$	combination angle
$\gamma_1$	yaw rate of tractor
$\delta_{_f}, \delta_{_r}, \delta_{_t}$	steering angles
$m_{1}, m_{2}$	mass of the tractor and trailer
$J_{z1}, J_{z2}$	tractor's moment of inertia and trailer's moment of
	inertia
$l_f, l_r$	distances from P to front and rear wheel axle of
	tractor
$l_t$	length of trailer
$d_{p}, d_{2}$	distances from the connector to P and C.G.
h	distance from P to C.G.
$C_{f}, C_{r}, C_{t}$	cornering stiffness

$$\begin{aligned} \dot{z}(t) &= A_{z}z(t) + B_{z}(\boldsymbol{u}(t) - \boldsymbol{b}\varepsilon_{c}(t)) \tag{1} \\ z(t) &= H_{p}^{T} \Big[ v_{p}(t) \quad \gamma_{1}(t) \quad \dot{\varepsilon}_{c}(t) \Big]^{T}, \, \boldsymbol{u}(t)^{T} = \Big[ \delta_{f}(t) \quad \delta_{r}(t) \quad \delta_{t}(t) \Big] \\ A_{z} &= -v_{x}D_{z} - v_{x}^{-1}B_{z}, \, B_{z} = QK, \, \boldsymbol{b}^{T} = \begin{bmatrix} 0 \quad 0 \quad 1 \end{bmatrix} \\ Q &= H_{p}^{T} \left( T^{T}M_{c}T \right)^{-1}H_{p}, \, K = \text{diag} \Big[ c_{f} \quad c_{r} \quad c_{t} \Big] \end{aligned}$$
(2)  
$$M_{c} = \begin{bmatrix} m_{1} + m_{2} & -m_{2}d_{3} & m_{2}d_{2} \\ -m_{2}d_{3} & J_{z3} + m_{2}d_{3}^{2} & -J_{z2} - m_{2}d_{2}d_{3} \\ m_{2}d_{2} & -J_{z2} - m_{2}d_{2}d_{3} & J_{z2} + m_{2}d_{2}^{2} \end{bmatrix} \end{aligned}$$
(3)  
$$D_{z} = H_{p}^{T} \begin{bmatrix} 0 \quad 1 \quad 0 \\ 0 \quad 0 \quad 0 \\ 0 \quad 0 \quad 0 \end{bmatrix} (H_{p}^{T})^{-1}, \, T = \begin{bmatrix} 1 \quad h \quad 0 \\ 0 \quad 1 \quad 0 \\ 0 \quad 0 \quad 1 \end{bmatrix}$$
(3)  
$$H_{p}^{T} = \begin{bmatrix} 1 \quad 1 & 1 \\ l_{f} \quad -l_{r} \quad -(d_{p} + l_{t}) \\ 0 \quad 0 \quad l_{t} \end{bmatrix}$$

Where  $d_1 = d_p + h, d_3 = d_1 + d_2$  and  $J_{z3} = J_{z1} + J_{z2}$ .  $M_c$  is a positive definite matrix.

The nominal values of combined vehicle are shown in Table 2.

## **III. IDEAL VEHICLE MODEL**

#### 1. Driver Model

In this paper, a linear preview driver model [8] is employed to describe the properties of drivers. In Fig.2, the solid lines represent the state of the combined vehicles, and the dashed lines represent the ideal state of the combined vehicles tracking the target lane.  $y_r(t)$  is the lateral distance between P and the target lane,  $\varepsilon_r(t) = \varepsilon_1(t) - \varepsilon_d(t)$  is the relative yaw angle between the vehicle and the target lane.  $\varepsilon_d(t)$  is the yaw angle of the ideal state,  $\rho(t)$  is the curvature of target lane. The predicted deviation  $\tilde{v}_{a}(t)$  is defined by

$$\widetilde{y}(t) = y_r(t) + T_p \dot{y}_r(t)$$
(4)
where T is the preview time constant v is the

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Fig.2 Driver-Vehicle-System

Therefore, the equation of the driver steering angle  $\delta_c(t)$  is given by

$$\tilde{T}_{s}\ddot{\mathcal{S}}_{c}(t) + \dot{\mathcal{S}}_{c}(t) = -g_{p}\tilde{\tilde{y}}(t) - g_{i}\tilde{y}(t)$$
(5)

where  $T_s$  is a steering time constant and denotes the reaction time delay of drives and mechanical systems,  $g_{p}, g_{i}$  is the steering gain. In this paper, we add an integrator to the driver model of [8] so that  $y_r(t)$  can converge to zero when the curvature of target lane is not zero.

#### 2. The Form of Ideal Vehicle Model

In the following explanation, *s* is Laplace variable, the symbols  $\mathcal{L}, \mathcal{L}^{-1}$  denote Laplace transform and inverse Laplace transform.

Based on the proposed ideal vehicle model proposed in [5], the form of ideal vehicle modes is proposed as

$$v_{pd}(t) = \mathcal{L}^{-1} \left[ \frac{g_v \omega_n^2 s}{A_M(s)} \mathcal{L}[v_x \delta_c(t)] \right]$$
  

$$\gamma_{1d}(t) = \mathcal{L}^{-1} \left[ \frac{g_v \omega_n^2 (\eta s + 1)}{A_M(s)} \mathcal{L}[v_x \delta_c(t)] \right]$$
  

$$A_M(s) = s^2 + 2\omega_n \zeta s + \omega_n^2$$
(6)

$$g_{v} = \overline{g}_{v} \frac{\overline{g}_{p}s + \overline{g}_{i}}{\hat{g}_{p}s + \hat{g}_{i}} \frac{\overline{T}_{p}s + 1}{\hat{T}_{p}s + 1}, g_{\gamma} = \overline{g}_{\gamma}(v_{x}) \frac{\overline{g}_{p}s + \overline{g}_{i}}{\hat{g}_{p}s + \hat{g}_{i}} \frac{\overline{T}_{p}s + 1}{\hat{T}_{p}s + 1} \right)$$

$$\mathcal{L}[\varepsilon_{cd}(t)] = \frac{\omega_{n}^{2}}{A_{M}(s)} \mathcal{L}[\delta_{ci}(t)], \varepsilon_{ci}(t) = \frac{2d_{p}v_{x}\gamma_{1d}(t)}{v_{x}^{2} - (d_{p}\gamma_{1d}(t))^{2}}$$
(7)

where  $\omega_n, \zeta, \eta, \overline{g}_{\nu}, \overline{g}_{\gamma}(v_x), \overline{g}_p, \overline{g}_i, \overline{T}_p$  are positive design parameters to be determined later.  $v_{pd}(t)$  is the ideal lateral velocity of the tractor,  $\gamma_{1d}(t)$  is the ideal combination yaw angle, and  $\varepsilon_{cd}(t)$  is the ideal combination yaw angle. In (6),  $\hat{g}_p, \hat{g}_i, \hat{T}_p$  are the estimated values of the steering gains  $g_{i}$ ,  $g_{i}$  and the preview time constant  $T_p$ . In the case of a constant driver steering angle, the desired lateral velocity  $v_{nd}(t)$ of the tractor converges to zero and the desired yaw rate  $\gamma_{1d}(t)$  of the tractor tends to a constant value  $\lim_{t \to \infty} \gamma_{1d}(t) = \overline{\gamma}_{1d}$ . Then, the tractor becomes tangent to the circular lane with the radius  $v_x / \overline{\gamma}_{1d}$  and travels.

In the actual combined vehicles using the adaptive steering controller, the property of the actual vehicles becomes as same as that of the ideal vehicle model. In this case, the following property can be obtained.

	Table 2	Nominal v			
$m_1$	1060	kg	$J_{z1}$	1507	kgm <sup>2</sup>
$l_f$	1.13	m	$l_r$	1.34	m
$d_p$	2.27	m	h	0	m
$d_2$	2.26	m			
$\mathcal{C}_{f}$	29700	N/rad	$C_r$	41460	N/rad
$m_2$	436	kg	$J_{z2}$	805	kgm <sup>2</sup>
$l_t$	2.48	m	$C_t$	100000	N/rad

$$Y_{r}(s) = \frac{-s(T_{s}s+1)A_{M}(s)v_{x}^{2}}{s^{3}(T_{s}s+1)A_{M}(s) + C(s)v_{x}\omega_{n}^{2}B_{M}(s)}\rho(s) + \frac{s^{2}(T_{s}s+1)A_{M}(s) + C(s)r_{p}v_{x}\omega_{n}^{2}B_{M}(s)}{s^{3}(T_{s}s+1)A_{M}(s) + C(s)v_{x}\omega_{n}^{2}B_{M}(s)}Y_{r}(0)$$

$$B_{M}(s) = \overline{g}_{v}s^{2} + v_{x}\overline{g}_{r}\eta s + v_{x}\overline{g}_{r}$$

$$C(s) = (\overline{g}_{p}s + \overline{g}_{i})(\overline{T}_{p}s+1)\frac{g_{p}s + g_{i}}{g_{p}s + g_{i}}\frac{T_{p}s + 1}{\hat{T}_{p}s + 1}$$

$$D(s) = (\overline{g}_{p}s + \overline{g}_{i})\frac{g_{p}s + g_{i}}{\hat{g}_{p}s + g_{i}}\frac{T_{p}s + 1}{\hat{T}_{p}s + 1}$$

$$(8)$$

From (8), it can be seen easily that if the estimated values  $\hat{g}_p$ ,  $\hat{g}_i$ ,  $\hat{T}_p$  are almost equal to the parameters  $g_p$ ,  $g_i$ ,  $T_p$  of actual vehicle, the variation of the property shown in (8) becomes small.

#### 3. Determination of Design Parameters

In the passive combined vehicles, the nominal values of vehicle parameters (see Table 2) are used. In the following explanation, the determination method of design parameters  $\omega_n, \zeta, \eta, \overline{g}_v, \overline{g}_\gamma(v_x), \overline{g}_p, \overline{g}_i, \overline{T}_p$  is shown.

**Step 1** In order that oscillation cannot occur in the desired trajectories of a ideal vehicle model,  $\zeta$  is set as  $\zeta = 1$ .

**Step 2** Using the average values of the driver parameters, the driver parameters  $g_p, g_i, T_p$  are set as  $g_p = 0.008, g_i = 0.0012, T_p = 2.2$ . In addition, it is assumed that  $g_p = \overline{g}_p = \hat{g}_p, g_i = \overline{g}_i = \hat{g}_i, T_p = \overline{T}_p = \hat{T}_p$ . **Step 3** For a constant longitudinal velocity  $v_x$ , we can

**Step 3** For a constant longitudinal velocity  $v_x$ , we can obtain the yaw rate gain as  $\overline{g}_{\gamma}(v_x) = \frac{3.06 \times 10^2}{7.59 \times 10^2 + 2.24 \times v_x(t)^2}$ . In order to make it easy for the ideal vehicle model to drive a corner, the design parameter  $\overline{g}_{\gamma}(v_x)$  is determined as

$$\overline{g}_{\gamma}(v_{x}) = \frac{1.8 \times 3.06 \times 10^{2}}{7.59 \times 10^{2} + 2.24 \times v_{x}(t)^{2}}$$
(9)

**Step 4** To design a vehicle model with good handling stability, an evaluation function is introduced by using the trail and error approach.

$$J = \int_{0}^{t} (2y_{r}(t)^{2} + 2y_{rr}(t)^{2} + 4\ddot{y}_{r}(t)^{2} + 4\ddot{\varepsilon}_{c}(t)^{2})dt + 3\max\ddot{y}_{r}(t) + 3\max\ddot{\varepsilon}_{c}(t)$$
(10)

Where *T* is the simulation time. Based on the evaluation function, the remaining design parameters  $\overline{g}_{v}, \eta, \omega_{n}$  are determined so that the following conditions can be satisfied.

(a) The imaginary part of the eigenvalues of  $B_M(s)$  is minimized preferably.

(b) The evaluation function is minimized preferably in lane change and cornering maneuver.

**Step 5** If the designed ideal vehicle model does not have good handling stability, we return to Step  $3\sim4$ .

As result,  $\overline{g}_v, \eta, \omega_n$  are set as  $\overline{g}_v = 0.25, \eta = 0.39$ ,  $\omega_n = 5.4$ . In the following part, using numerical simulations, the property of designed the ideal vehicle model is shown. In the lane change maneuver, the curvature of target lane is  $\rho(t) = 0$ [m]. The initial value of  $y_r(t)$  is set as  $y_r(0) = -3.0$ [m]. In the cornering maneuver, the curvature of target lane is  $\rho(t) = 1/500$ [m]. The initial value of  $y_r(t)$  is set as  $y_r(0) = -1.0$ [m]. Until now, from many research results, the value of  $T_s$  is obtained as  $0.05 \sim 0.4$ [s]. For this reason, in the following numerical simulations, we check controlled performance in  $0.05 \le T_s \le 0.4$ [s].

At first, the effectiveness of the proposed ideal vehicle model is shown in the lane change maneuver. In the case of varying  $v_x$  and  $T_s$ , the variation of J is shown in Figure 3. Fig.3 (a) shows the values of J for the passive combined vehicle, Fig.3 (b) shows the values of J for the adaptive steering driver vehicle system using the proposed ideal vehicle model. Hereafter, it is called the adaptive vehicle simply. In Fig.3, in case where J exceeds 80, the values of J are shown as 80. As shown Fig.3 (a), there exists a region in which J exceed 80. In the region, the handling performance of the passive vehicle becomes unstable. However, as shown in Fig.3 (b), for the adaptive vehicle, the values of J are less than 70 and good handling performance can be achieved.

Next, the effectiveness of the proposed ideal vehicle model is shown in the cornering maneuver. In the case of varying  $v_x$  and  $T_s$ , the variation of J is shown in Figure 4. Fig.4 (a) shows the values of J for the passive combined vehicle, Fig.4 (b) shows the values of J for the adaptive vehicle. In Fig.4, in case where J exceeds 35, the values of J are shown as 35. As shown Fig.4 (a), there exists a region in which J exceeds 35. In the region, the handling performance of the passive vehicle becomes unstable. However, as shown in Fig.4 (b), for the adaptive vehicle, the values of J are less than 21 and good handling performance can be achieved.

Moreover, we show the effectiveness of the proposed ideal vehicle in the presence of the estimated errors in  $\hat{g}_p$ ,  $\hat{g}_i$ ,  $\hat{T}_p$ . In case where the values of  $g_p / \hat{g}_p$  and  $g_i / \hat{g}_i$  are not equal to one, we can obtain the similar graphs to Fig.3 (b) and Fig.4 (b). For each values of  $g_p / \hat{g}_p$  and  $g_i / \hat{g}_i$ , the maximum value of Fig.3 (b) is plotted in Fig.5 (a) and the maximum value of Fig.4 (b) is plotted in Fig.5 (b). Similarly, for each values of  $T_p / \hat{T}_p$ , the maximum values of Fig.3 (b), Fig.4 (b) are plotted in Fig.6.

As shown in Fig.5, in the region of  $0.6 \le g_p / \hat{g}_p \le 1.4$  and  $0.8 \le g_i / \hat{g}_i \le 1.6$ , the values of *J* became less than 75 in the lane change maneuver and



the values of J became less than 30 in the cornering maneuver. As shown in Fig.6, in the region of  $0.7 \le T_p / \hat{T}_p \le 1.3$ , the values of *J* became less than 75 in the lane change maneuver and the values of J became less than 25 in the cornering maneuver. From the facts, it can be concluded that the proposed ideal vehicle model is very effective when the estimated values of the driver parameters are within the regions  $0.6 \le g_p / \hat{g}_p \le 1.4, 0.8 \le g_i / \hat{g}_i \le 1.6 \text{ and } 0.7 \le T_p / T_p \le 1.3$ . Namely, it can be seen that accurate values of the driver parameters are not required.

## **IV. CONCLUSION**

In this paper, we propose a design method to design not several ideal vehicle models but only one ideal vehicle model against variations of the driver properties. Carrying out numerical simulations, it is shown that the handling performance in the adaptive driver vehicle system is far better than that of passive combined vehicle. Moreover, it is also shown that in the design scheme of an ideal vehicle model, rough information of the driver properties are only required to maintain good handling performance.

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Fig.6 Variation maximum value of J for various  $T_{n}$ 

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